Sec 1H Opener for January 8, 2019

$$
f(x)=2 x-6 \quad g(x)=x+4 \quad \mid(x+4)
$$

1. What is VERTICAL SHIFT for $g(x)$ ? $\square$
2. What is VERTICAL STRETCH for $f(x)$ ?
3. What is HORIZONTAL SHIFT for $f(x)$ ?

$$
2(x-3)+3
$$

4. Write $f(x) g(x)$.

$$
f(x) G(x)=(2 x-6)(x+4)
$$

5. What are the $x$-intercepts for $f(x) g(x)$ ?


Bonus: What is the $y$-intercept? $(0,-24)$

### 8.2H Lines are a Changin'

SHOW YOUR WORK. WORK IN PENCIL.

1. Use the graph below of the functions to answer the questions
a. Fill in the table from the graph below for $f(x)$ and $g(x)$
b. Plot the points for $f(\mathrm{x})+g(\mathrm{x})$ in one color and $f(\mathrm{x}) g(\mathrm{x})$ in a different color.
c. What kind of graph is made by $f(\mathrm{x})+g(\mathrm{x})$ ? $\qquad$
d. Write the equation for $f(x)+g(x)$ ? $\qquad$
$\qquad$
e. Where does $f(\mathrm{x})=g(\mathrm{x})$ ?
f. Write the equation for $f(\mathrm{x})$ $\qquad$
$\qquad$
$\qquad$
$\qquad$
h. Where do you see this in your equation? $\qquad$
i. Look at the graph, what's the $x$-int for $f(x)$ $\qquad$
Change your equation to expose the $x$-int
out the slope to look like: $y=m\left(x+\frac{b}{m}\right)$.
Write the equation for $g(x)$ $\qquad$
2. What is the slope for $g(x)$ : $\qquad$
m . Where do you see this in your equation?
n. What is the x-intercept for $g(x)$ : $\qquad$
$\qquad$
o. Change your equation to show the $x$-intercept.
p. What is $f(4)+g(4)$ ?
q. What kind of graph is made by $f(\mathrm{x}) g(\mathrm{x})$ ? $\qquad$
r. What are your x-intercepts for $f(\mathrm{x}) g(\mathrm{x})$ $\qquad$
s. Write an equation in factored form for $f(\mathrm{x}) g(\mathrm{x})$ based on " $q$ " above. $\qquad$ Questions?? per $\qquad$ Name $\square$

| x | $f(\mathrm{x})$ | $g(\mathrm{x})$ | $f(\mathrm{x})+g(\mathrm{x})$ | $f(\mathrm{x}) g(\mathrm{x})$ |
| :---: | :---: | :---: | :---: | :---: |
| -2 |  |  |  |  |
| -4 |  |  |  |  |
| 2 |  |  |  |  |
| 0 |  |  |  |  |
| -5 |  |  |  |  |
| 4 |  |  |  |  |

t. What is $g(-2) f(-2)$ ? $\qquad$

2. Given the equation $h(x)=4 x+12 .-4 x-8$
a. Fill in a table of values using the equation.

From the parent graph $f(\mathrm{x})=\mathrm{x}$ :
b. What is the vertical stretch of $h(\mathrm{x})$ ?
c. Where do you see the vertical stretch in the equation?
d. What is the vertical shift of $h(\mathrm{x})$ ?
$\qquad$
$\qquad$ -
e. Where do you see the vertical shift in the equation? $\qquad$
f. Factor out the slope for $h(x)$. $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
i. What change would happen if x became $(\mathrm{x}+3)$, or $h(x+3)$ ?
j. How would you make all the points on the line move down 8 units?
k. Write the equation for your new line above: $\qquad$

1. Show your equation that would show your new $x$-intercepts
m . How would the vertical stretch change?
2. Compare the three equations $f(\mathbf{x})=5 \mathrm{x}+15$ and $d(\mathbf{x})=3 \mathrm{x}+\mathbf{6}$ and $f(\mathbf{x})+d(\mathbf{x})$.
a. How you would express $f(\mathrm{x})+d(\mathrm{x})$ as an equation? $\qquad$
$\qquad$
b. Which of the three equations has the greatest vertical shift? $\qquad$
c. How do you know? $\qquad$
$\qquad$ -
e. Which equation has the greatest horizontal shift left? $\qquad$
f. How do you know?
?
g. Which equation has the greatest vertical stretch?
h. How do you know?
3. Given the equations $f(x)=2 x+5$ and $d(x)=3 x+2$, find:
a. $f(\mathrm{x})+d(\mathrm{x})=$
b. $f(\mathrm{x})-d(\mathrm{x})=$
e. Write an equation (do not solve) for $f(\mathrm{x}) d(\mathrm{x})$
c. if $\mathrm{x}=1, f(\mathrm{x})+d(\mathrm{x})=$
f. If $\mathrm{x}=-1, f(\mathrm{x}) d(\mathrm{x})=$
d. If $\mathrm{x}=2, f(\mathrm{x})-d(\mathrm{x})=$
4. Given the equations $f(x)=x+4$ and $d(x)=2 x+5$, find:
a. $\quad f(\mathrm{x})+d(\mathrm{x})$
d. $f(-2)-d(3)$
b. $f(\mathrm{x})-d(\mathrm{x})$
c. $\quad f(1)+d(2)$
e. Write an equation (do not solve) for $f(\mathrm{x}) d(\mathrm{x})$
. $f(4) \times d(2)$
g. Write an equation (do not solve) for $\frac{f(x)}{d(x)}$
h. $\frac{f(2)}{d(1)}$
5. Mrs. Burton took her pet snail to Boston to enroll her at MIT. While on the commons, Esmargo crept to the top of the dome in the quad at point $(1,6)$.
a. Describe the path Esmargo took if she crept along the slope triangle of the grid below.
b. Using math, what happened to the $x$ value?
c. What happened to the $y$ value? $\qquad$
d. Write this shorthand in a coordinate point:
e. What distance did Esmargo slither if she climbed up the hypotenuse of your slope triangle. $\qquad$
From the dome, Esmargo decided to rest under the
 math notation as above).
g. Write an equation (do not solve) for $\frac{f(x)}{d(x)}$
h. If $\mathrm{x}=2, \frac{f(x)}{d(x)}=$
$\qquad$
g. How far did she slither from the top of the dome to under the tree? SYW. $\qquad$
$\qquad$ SHOW YOUR WORK. WORK IN PENCIL.

Uerte enestions
Use the graph below of the functions to answer the question
a. Fill in the table from the graph below for $f(\mathrm{x})$ and $g(\mathrm{x})$ Fill in the table from the graph below for $f(\mathrm{x})$ and $g(\mathrm{x})$
Plot the points for $f(\mathrm{x})+g(\mathrm{x})$ in one color and $f(\mathrm{x}) g(\mathrm{x})$ in a different color.
c. What kind of graph is made by $f(x)+g(x)$ ? linear
d. Write the equation for $f(\mathrm{x})+g(\mathrm{x})$ ? $X-2$
e. Where does $f(\mathrm{x})=g(\mathrm{x})$ ?
f. Write the equation for $f(x)$ : $\qquad$
$\qquad$

g. What is the y-intercept for $f(\mathrm{x})$ : $\quad(0,2$
h. Where do you see this in your equation? constant
i. Look at the graph, what's the $x$-int for $f(x):(-1,0)$
j. Change your equation to expose the x -int by factoring out the slope to look like: $y=m\left(x+\frac{b}{m}\right), 2(X+1)$
k. Write the equation for $g(x):-X-4$

1. What is the slope for $g(x)$ : $\qquad$ $-1$
m. Where do you see this in your equation? coefficient
n. What is the x-intercept for $g(x)$ :

o. Change your equation to show the $x$-intercept. $-1(x+4)$
p. What is $f(4)+g(4)$ ? $\qquad$ by $f(\mathrm{x}) g(\mathrm{x})$ parabota
q. What kind of graph is made by $f(\mathrm{x}) g(\mathrm{x}) ?$ parabola
r. What are your x -intercepts for $f(\mathrm{x}) g(\mathrm{x})(-4,0)(-1,0)$
s. Write an equation in factored form for $f(\mathrm{x}) g(\mathrm{x})$ based on "q" above. $(2 x+2)(-x-4)$
What is $g(-2) f(-2)$ ? $\qquad$

| x | $f(\mathrm{x})$ | $g(\mathrm{x})$ | $f(\mathrm{x})+g(\mathrm{x})$ | $f(\mathrm{x}) g(\mathrm{x})$ |
| :---: | :---: | :---: | :---: | :---: |
| -2 | -2 | -2 | -4 | 4 |
| -4 | -6 | 0 | -6 | 0 |
| 2 | 6 | -6 | 0 | -36 |
| 0 | 2 | -4 | -2 | -8 |
| -5 | -8 | 1 | -7 | -8 |
| 4 | 10 | -8 | 2 | -80 |

t. What is $g(-2) f(-2)$ ? $\qquad$

2. Given the equation $h(x)=4 x+12 .-4 x-8$

2 a. Fill in a table of values using the equation. From the parent graph $f(\mathrm{x})=\mathrm{x}$ :
b. What is the vertical stretch of $h(\mathrm{x})$ ? $\qquad$ $-4$
c. Where do you see the vertical stretch in the equation? slope
d. What is the vertical shift of $h(\mathrm{x})$ ? $\qquad$
e. Where do you see the vertical shift in the equajion? $y$-int, constant

f. Factor out the slope for $h(x) \cdot-4(x+2)$
g. What is the horizontal shift of $h(x) ?-2$
g. What is the horizontal shift of $h(x)$ ? -2
h. Where do you see the horizontal shift in the equation? add to $x$ in factor form
i. What change would happen if $x$ became $(x+3)$, or $h(x+3)$ ? shift Lft 3
j. How would you make all the points on the line move down 8 units?
-8from $y$ - int
k. Write the equation for your new line above $\qquad$

1. Show your equation that would show your new $x$-intercept $-4 . x+4$
m . How would the vertical stretch change? $\qquad$
2. Compare the three equations $f(x)=5 x+15$ and $d(x)=3 x+6$ and $f(x)+d(x)$.

10 a. How you would express $f(\mathrm{x})+d(\mathrm{x})$ as an equation?
. How of the three equations has the greatest vertical
d. Factor the vertical stretch from all three equations: $3(x+2)$

S - - - 2
e. Which equation has the greatest horizontal shift left?
f. How do you know? $\qquad$ est x $f(x)+d(x)$
g. Which equation has the greatest vertical stretch?
h. How do you know? __ argest slope
4. Given the equations $f(x)=2 x+5$ and $d(x)=3 x+2$, find:
a. $f(\mathrm{x})+d(\mathrm{x})=$
$5 x+7$
e. Write an equation (do not
b. $f(\mathrm{x})-d(\mathrm{x})=$
$-x+3$
c. if $\mathrm{x}=1, f(\mathrm{x})+d(\mathrm{x})=$

g. Write an equation (do no ${ }^{t}$ -
solve) for $\frac{f(x)}{d(x)}$
h. If $\mathrm{x}=2, \frac{f(x)}{d(x)}=$

d. If $\mathrm{x}=2, f(\mathrm{x})-d(\mathrm{x})=$
f. If $\mathrm{x}=-1, f(\mathrm{x}) d(\mathrm{x})=$
5. Given the equations $f(x)=x+4$ and $d(x)=2 x+5$, find:
$f(\mathrm{x})+d(\mathrm{x})$
d. $f(-2)-d(3)$

- 9
b. $f(\mathrm{x})-d(\mathrm{x})$
$-X-1$
e. Write an equation (do not
c. $\quad f(1)+d(2)$

$$
\begin{aligned}
& \text { solve }) \text { for } f(x) d(x) \\
& (x+4) 2 x+5
\end{aligned}
$$

14
f. $\quad f(4) \times d(2)$
72
6. Mrs. Burton took her pet snail to Boston to enroll her at MIT. While on the commons, Esmargo crept to the top of the 7 dome in the quad at point $(1,6)$.
a. Describe the path Esmargo took if she crept along the slope triangle of the grid below. $\qquad$
b. Using math, what happened to the $x$ value?
c. What happened to the $y$ value? $\qquad$ $+13$
d. Write this shorthand in a coordinate point: $\mathbf{-}^{-}, 13$
e. What distance did Esmargo slither if she climbed up the hypotenuse of your slope triangle. $\qquad$
f. From the dome, Esmargo decided to rest under the little tree at $(-5,-6)$. Describe her path (using the math notation as above). $\qquad$ $6-12$
g. How far did she slither from the top of the dome to under the tree? SYW $\qquad$

## Multiplying Polynomials

There are four methods we will show you.

- Stacking Method
- Box Method
- Distributive Method
- FOIL

STACKING METHOD

$$
\begin{gathered}
(3 x+7)(x-5) \\
3 x+7 \\
\frac{x-5}{-15 x-35} \\
3 x^{2}+7 x \\
\frac{3 x^{2}-8 x-35}{1 .(2 x-3)(3 x+2)} \\
6 x^{2}-5 x-6 \\
\text { 2. }(4 s+3)(s-7) \\
4 s^{2}-25 s-21
\end{gathered}
$$

BOX METHOD

$(t+4)(t+2)$

2. $(r+1)(r+6)$
$r^{2}+7 r+6$


DISTRIBUTIVE METHOD
To distribute means to multiply every term in the parentheses. The same applies to binomials and polynomials.

$$
\begin{aligned}
& 6(x-2)=6 * x-6 * 2=6 x-12 \\
& (x+4)(x-5) \\
& x(x-5)+4(x-5) \\
& x^{2}-5 x+4 x-20 \\
& \text { 1. }(x+9)(x+5) \quad x^{2}-x-20 \\
& x(x+5)+9(x+5) \\
& \text { 2. }(x-1)(x-4) \quad x^{2}+14 x+40 \\
& x^{2}-5 x+4
\end{aligned}
$$

## FOIL

## Eirst Outside Inside Last

This is just a specific application of binomials and the distributive property.


1. $(x+3)(x-1)$
2. $(2 x-1)(x-4)$

## Your Turn

Using the method of your choice, multiply the following:

1. $(3 x+2)(x+5)$
2. $(x+12)(x+2)$

Bonus: $\left(2 x^{2}+4 x+5\right)\left(3 x^{2}+x+9\right)$ SHOW WORK!

